

Electronic structure of BiMeO_3 multiferroics and related oxides

J. A. McLeod,¹ Z. V. Pchelkina,² L. D. Finkelstein,² E.Z. Kurmaev,² R. G. Wilks,¹
A. Moewes,¹ I. V. Solovyev,^{2,3} A. A. Belik,⁴ and E. Takayama-Muromachi⁴

¹*Department of Physics and Engineering Physics,
University of Saskatchewan, 116 Science Place,
Saskatoon, Saskatchewan S7N 5E2, Canada**

²*Institute of Metal Physics, Russian Academy of Sciences-Ural Division,
620041 Yekaterinburg GSP-170, Russia[†]*

³*Computational Materials Science Center,
National Institute for Materials Science,
1-2-1 Sengen, Tsukuba, Ibaraki 305-0047, Japan*

⁴*International Center for Materials Nanoarchitectonics (MANA),
National Institute for Materials Science (NIMS),
1-1 Namiki, Tsukuba, Ibaraki 305-0044, Japan*

(Dated: October 1, 2009)

Abstract

We have performed a systematic study of the electronic structures of BiMeO_3 ($Me = \text{Sc, Cr, Mn, Fe, Co, Ni}$) series by soft X-ray emission (XES) and absorption (XAS) spectroscopy. The band gap values were estimated for all compounds in the series. For BiFeO_3 a band gap of ~ 0.9 eV was obtained from the alignment of the O K_α XES and O $1s$ XAS. The O $1s$ XAS spectrum of BiNiO_3 indicates that the formation of holes is due to a Ni^{2+} valency rather than a Ni^{3+} valency. We have found that the O K_α XES and O $1s$ XAS of BiMeO_3 probing partially occupied and vacant O $2p$ states, respectively, are in agreement with the O $2p$ densities of states obtained from spin-polarized band structure calculations. The O K_α XES spectra show the same degree of Bi $6s$ —O $2p$ hybridization for all compounds in the series. We argue herein that the stereochemical activity of Bi $6s$ lone pairs must be supplemented with inversion symmetry breaking to allow electric polarization. For BiMnO_3 and BiFeO_3 , two cases of multiferroic materials in this series, the former breaks the inversion symmetry due to the antiferromagnetic order induced by particular orbital ordering in the highly distorted perovskite structure and the latter has rhombohedral crystal structure without inversion symmetry.

I. INTRODUCTION

Multiferroics, discovered almost 50 years ago^{1,2}, are materials that simultaneously possess two or three degrees of freedom: (anti)ferromagnetism, (anti)ferroelectricity, and/or ferroelasticity, which allow both charge and spin to be manipulated by applied electrical and magnetic fields^{3,4}. These materials are promising for various technological applications such as information storage, spintronics, and sensors. There are many different classes of multiferroic systems known today, for instance: the $RMnO_3$ family ($R = \text{Dy, Tb, Ho, Y, Lu, etc.}$), the RMn_2O_5 family ($R = \text{Nd, Sm, Dy, Tb}$), and the $BiMeO_3$ family ($Me = \text{Mn, Fe}$). These materials have complex structures with many atoms per formula unit, and more than one formula unit per unit cell. The large number of interatomic interactions makes distinguishing the mechanisms responsible for multiferroicity a challenging task. The origin of these phenomena and the nature of the coupling between the magnetic, electric, and structural order parameters are not well understood. Despite many electronic structure calculations (see review article 5 and references therein) only few experimental spectra for selected compounds ($YMnO_3$ and $BiFeO_3$) have so far been obtained^{6,7}. In order to get deeper insight into the nature of multiferroicity we have performed a systematic study of electronic structure of the perovskite-like multiferroics ($BiFeO_3$ and $BiMnO_3$) and the $BiMeO_3$ ($Me = \text{Sc, Cr, Co, Ni}$) related compounds using synchrotron excited soft X-ray emission and absorption spectra. The experimental results are compared with specially performed electronic structure calculations.

The paper is organized as follows: the details of sample preparation and X-ray measurements are presented in Section II. The crystal structure of different compounds and their basic properties are summarized in Section III. Results of X-ray measurements for the whole series of $BiMeO_3$ ($Me = \text{Sc, Cr, Fe, Co, Ni}$) compounds and comparison with electronic structure calculations are collected in Section IV.

II. EXPERIMENTAL DETAILS

All the samples were synthesized using a high-pressure high-temperature method. Starting mixtures were placed in Au capsules and treated at 6 GPa in a belt-type high-pressure apparatus at different temperatures (heating rate was about 140 K/min). After heat treat-

ment, the samples were quenched to room temperature (RT), and the pressure was slowly released. BiCrO_3 was prepared from mixtures of Bi_2O_3 (99.99 %) and Cr_2O_3 (99.9 %) with an amount-of-substance ratio of 1:1 at 1653 K for 60-70 min⁸. BiMnO_3 was prepared from mixtures of Bi_2O_3 and Mn_2O_3 with an amount-of-substance ratio of 1:1 at 1383 K for 60-70 min⁹. Single-phased Mn_2O_3 was prepared by heating commercial MnO_2 (99.99 %) in air at 923 K for 24 h. For the preparation of BiScO_3 , stoichiometric mixtures of Bi_2O_3 and Sc_2O_3 (99.9 %) were dried at 873 K for 8 h and then treated at 1413 K (at 6 GPa) for 40 min¹⁰.

For the preparation of BiFeO_3 , stoichiometric mixtures of Bi_2O_3 and Fe_2O_3 (99.9 %) were first annealed at ambient pressure at 1073 K for 2 h. This procedure gave a mixture of BiFeO_3 (about 70 weight %), $\text{Bi}_{25}\text{FeO}_{39}$, and $\text{Bi}_2\text{Fe}_4\text{O}_9$. The resulting mixture was treated at 1273 K (at 6 GPa) for 1 h. After the high-pressure treatment, single-phased BiFeO_3 was obtained. BiCoO_3 was synthesized from stoichiometric mixtures of Bi_2O_3 , Co_3O_4 (99.9 %), and KClO_3 at 1483 K (at 6 GPa) for 1 h, and BiNiO_3 from Bi_2O_3 , NiO (99.9 %), and KClO_3 at 1483 K (at 6 GPa) for 1 h. The resulting samples were reground, washed with water, dried, and re-pressed at about 1 GPa at room temperature.

The X-ray emission spectra (XES) were measured at beamline 8.0.1 at the Advanced Light Source (ALS) at the Lawrence Berkeley National Laboratory¹¹. The X-ray absorption spectra (XAS) were measured at the Spherical Grating Monochromator beamline at the Canadian Light Source (CLS) at the University of Saskatchewan¹². The O $1s$ XAS spectra were measured in the total fluorescence yield (TFY) mode, which provides more bulk sensitivity than electron yield methods do. The O K_α XES was excited near the O $1s$ ionization threshold to suppress the high-energy satellite structure. The instrumental resolving power ($E/\Delta E$) was approximately 10^3 for the XES measurements and approximately 5×10^3 for the XAS measurements.

III. CRYSTAL STRUCTURE AND PHYSICAL PROPERTIES OF BiMeO_3 COMPOUNDS

Of all the multiferroic compounds, the most extensive study has been devoted to the perovskite-type and related oxides. Below we give a short summary of crystal structure and basic physical properties of the BiMeO_3 ($Me = \text{Sc, Cr, Mn, Fe, Co, Ni}$) compounds. The space groups and lattice constants for the whole series are collected in Table I. The selected

bond lengths are shown in Tables II, III and IV.

The structure of BiScO₃ has monoclinic symmetry with the space group $C2/c$ ¹⁰. BiScO₃ is nonmagnetic and most of the interest in this compound is in the ferroelectric properties of the BiScO₃-PbTiO₃ system. For the well known piezoelectric material Pb(Zr,Ti)O₃ (PZT) the Curie temperature T_C at the morphotropic phase boundary between the rhombohedral and tetragonal ferroelectric state is 386° C. It has been shown that for BiScO₃-PbTiO₃ the T_C reaches 450° C¹³ while the piezoelectric coefficients in bulk are comparable to those of commercial PZT.

BiCrO₃ crystallizes in an orthorhombic structure above 420 K with the space group $Pnma$ and lattice parameters $a = 5.54568(12)$ Å, $b = 7.7577(2)$ Å, $c = 5.42862(12)$ Å at 490 K⁸. A structural phase transition from an orthorhombic to a monoclinic structure occurs at 420 K^{8,14,15,16}. Between 420 K and 7 K BiCrO₃ has a monoclinic structure with the space group $C2/c$ and $a = 9.4641(4)$ Å, $b = 5.4790(2)$ Å, $c = 9.5850(4)$ Å, $\beta = 108.568(3)^\circ$ at 7 K⁸. A long-range G-type antiferromagnetic order with weak ferromagnetism develops below $T_N = 109$ K and does not change down to 7 K⁸. Four anomalies of magnetic origin were observed at 40, 75, 109 and 111 K¹⁶. Magnetic moments of Cr³⁺ ions were found to align along the monoclinic b axis in a similar manner to the direction of magnetic moments of Mn³⁺ in BiMnO₃^{17,18}. The magnetic structure of BiCrO₃ was first predicted from *ab initio* electronic structure calculations¹⁹.

TABLE I: Crystal structure and lattice parameters for BiMeO₃ compounds.

	BiScO ₃	BiCrO ₃	BiMnO ₃	BiFeO ₃	BiCoO ₃	BiNiO ₃
space group	$C2/c$	$C2/c$	$C2/c$	$R3c$	$P4mm$	$P\bar{1}$
a , [Å]	9.8899(5)	9.4641(4)	9.5415(2)	5.58102(4)	3.71990(7)	5.3852(2)
b , [Å]	5.8221(3)	5.4790(2)	5.61263(8)	5.58102(4)	3.71990(7)	5.6498(2)
c , [Å]	10.0462(5)	9.5850(4)	9.8632(2)	13.8757(2)	4.71965(15)	7.7078(3)
α , [°]	90	90	90	90	90	91.9529(10)
β , [°]	108.300(3)	108.568(3)	110.6584(12)	90	90	89.8097(9)
γ , [°]	90	90	90	120	90	91.5411(9)

The bismuth manganite (BiMnO₃) has a highly distorted perovskite structure and has been regarded as a multiferroic material. The ferroelectricity has been analyzed within

TABLE II: Selected bond lengths in BiScO₃, BiCrO₃ and BiMnO₃, in Å. $\Delta = \frac{1}{N} \sum_1^N (\frac{l_i - l_{av}}{l_{av}})^2$, and $l_{av} = \frac{1}{N} \sum_1^N l_i$, where l_i is the i-th bond.

	BiScO ₃	BiCrO ₃	BiMnO ₃
<i>Me</i> 1-O2x2	2.08570	1.98308	1.90556
<i>Me</i> 1-O1x2	2.10990	1.99158	2.19906
<i>Me</i> 1-O3x2	2.15779	1.97805	1.98549
$\Delta(\textit{Me}1\text{-O})$	2.0×10^{-4}	0.08×10^{-4}	37.2×10^{-4}
<i>Me</i> 2-O3x2	2.09607	1.97890	1.94151
<i>Me</i> 2-O1x2	2.11635	1.99268	1.92401
<i>Me</i> 2-O2x2	2.13574	2.01393	2.24174
$\Delta(\textit{Me}2\text{-O})$	0.6×10^{-4}	0.5×10^{-4}	51.3×10^{-4}
Bi-O3	2.15352	2.25697	2.24562
Bi-O2	2.19212	2.23752	2.21778
Bi-O1	2.24633	2.32584	2.23928
Bi-O1	2.55437	2.44659	2.46625
Bi-O3	2.89682	2.65246	2.70996
Bi-O2	3.01816	2.78741	2.83703
$\Delta(\text{Bi-O})$	18.7×10^{-3}	7.0×10^{-3}	9.9×10^{-3}

TABLE III: Selected bond lengths in BiFeO₃ and BiCoO₃, in Å.

Fe-Ox3	1.97139	Co-O1	1.71781
Fe-Ox3	2.08310	Co-O2x4	2.01593
$\Delta(\textit{Me}\text{-O})$	8×10^{-4}		37×10^{-4}
Bi-Ox3	2.30512	Bi-O2x4	2.25155
Bi-Ox3	2.51513	Bi-O1x4	2.79852
$\Delta(\text{Bi-O})$	1.9×10^{-3}		11.7×10^{-3}

first-principles electronic structure calculations²⁰, and attributed to the chemical activity of the Bi $6s^2$ lone pairs²¹. BiMnO₃ is the only ferromagnet among the discussed Bi*Me*O₃ compounds with a Curie temperature above 100 K. The largest saturation magnetization has been reported to be $3.92 \mu_B$ per formula unit⁹, which is close to the $4 \mu_B$ expected for the

TABLE IV: Selected bond lengths in BiNiO₃, in Å.

Ni1-O2x2	1.98294	Ni2-O3x2	2.04959	Ni3-O5x2	1.98075	Ni4-O1x2	2.05408
Ni1-O3x2	1.99200	Ni2-O4x2	2.07097	Ni3-O2x2	2.10662	Ni4-O6x2	2.10927
Ni1-O4x2	2.28697	Ni2-O1x2	2.13415	Ni3-O6x2	2.12071	Ni4-O5x2	2.20769
$\Delta(Me-O)$	46×10^{-4}		3×10^{-4}		9×10^{-4}		9×10^{-4}
Bi1-O3	2.21311	Bi2-O1	2.03349				
Bi1-O5	2.26541	Bi2-O4	2.04058				
Bi1-O2	2.32491	Bi2-O6	2.09686				
Bi1-O3	2.41745	Bi2-O2	2.13787				
Bi1-O1	2.52033	Bi2-O5	2.24213				
Bi1-O4	2.67658	Bi2-O6	2.25756				
$\Delta(Bi-O)$	4.3×10^{-3}		1.7×10^{-3}				

ferromagnetic state. The ferroelectric hysteresis loop has been observed in polycrystalline and thin film samples of BiMnO₃²², although the measured ferroelectric polarization was much smaller (about 0.043 $\mu\text{C}/\text{cm}^2$ at 200 K) than the one obtained in the first principle calculations for the experimental noncentrosymmetric structure (about 0.52 $\mu\text{C}/\text{cm}^2$)²³.

BiMnO₃ undergoes two phase transitions at temperatures 474K (monoclinic-monoclinic) and 770K (monoclinic-orthorhombic)^{24,25,26}. According to early experimental data BiMnO₃ was considered to have noncentrosymmetric $C2$ space group below 770 K^{24,25}. Recently the crystal structure of BiMnO₃ was re-examined by Belik *et al.*⁹ and confirmed by neutron powder diffraction experiments by Montanari *et al.*¹⁷. The new experiments reveal that BiMnO₃ below 770 K has a centrosymmetric $C2/c$ space group with parameters given in Table I. A structural optimization performed using modern methods of electronic structure calculations has shown that the noncentrosymmetric $C2$ structure, which had been reported earlier converges to the new total energy minimum corresponding to the $C2/c$ structure with zero net polarization^{27,28}.

Since the $C2/c$ structure of BiMnO₃ has inversion symmetry the hypothesis that electric polarization arises due to bismuth lone pairs is no longer valid. The magnetic mechanism of inversion symmetry breaking was considered recently in work 29. It was shown that the peculiar orbital ordering realized below 474 K gives rise to ferromagnetic (FM) interactions

between nearest-neighbor spins which compete with longer-range antiferromagnetic (AFM) interactions. The solution of the low-energy model for $3d$ states in BiMnO_3 revealed that the true symmetry is expected to be Cc . The solution of the realistic model indicates a non-collinear magnetic ground state, where the ferromagnetic order along one crystallographic axis coexists with the the hidden AFM order and a related ferroelectric polarization along two other axes³⁰.

The perovskite BiFeO_3 is ferroelectric with $T_c = 1103$ K and antiferromagnetic with $T_N = 643$ K and a canted spin structure³¹. The bulk single crystal has a rhombohedrally distorted perovskite structure with the space group $R\bar{3}c$ ³² and lattice parameters presented in Table I. The G-type collinear antiferromagnetic spin configuration has been modified by subjecting it to a long-range (620 Å) modulation leading to a spiral modulated spin structure³³. The spontaneous polarization of a single crystal is $3.5 \mu\text{C}/\text{cm}^2$ along (001) direction and $6.1 \mu\text{C}/\text{cm}^2$ in (111) direction at 77 K³⁴. This value is significantly smaller than spontaneous polarization of lead titanate (80 to $100 \mu\text{C}/\text{cm}^2$ with the $T_C \sim 763$ K). However the heteroepitaxially constrained thin films of BiFeO_3 display a room-temperature spontaneous polarization of $50\text{-}60 \mu\text{C}/\text{cm}^2$, an order of magnitude higher than in the bulk³⁵. The spin polarized first-principles calculation within local spin density approximation (LSDA) using the pseudopotential VASP package with the optimized lattice parameters for the bulk rhombohedral phase results in polarization of $6.61 \mu\text{C}/\text{cm}^2$ ²³⁵ in excellent agreement with experiment. The thin films were shown to have tetragonal-like structure. For the $P4mm$ symmetry and lattice parameters measured for thin film the Barry-phase calculation yields a spontaneous polarization of $63.2 \mu\text{C}/\text{cm}^2$ ²³⁵, consistent with experimental data, but it was revealed that small changes of lattice parameters can lead to a dramatically different polarization. The magnetoelectric coefficient (dE/dH , E - electric field, H - magnetic field) was measured to be $3 \text{ V}/\text{cm}\cdot\text{Oe}$ at zero field³⁵. Later on the values of remnant polarization were increased to $55 \mu\text{C}/\text{cm}^2$ for (001) films, $80 \mu\text{C}/\text{cm}^2$ for (101) films and about $100 \mu\text{C}/\text{cm}^2$ for (111) films³⁶. The BiFeO_3 films grown on (111) have the rhombohedral structure as single crystals, whereas films grown on (101) or (001) are monoclinically distorted³⁶. The highest remnant polarization ever measured for a ferroelectric material, $146 \mu\text{C}/\text{cm}^2$, has been reported for BiFeO_3 thin films with tetragonal crystal structure in work³⁷. A wide range of measured polarization values were shown to be in consistent with the modern theory of polarization^{38,39,40}, which recognizes that polarization is a lattice of values rather than a

single vector⁴¹.

BiCoO₃ is isotypic with BaTiO₃ and PbTiO₃ and has a tetragonal crystal structure with the lattice parameters $a = 3.71990(7)$ Å, $b = 4.71965(15)$ Å, $c/a = 1.269$ at 5K⁴². BiCoO₃ is an insulator with $T_N = 470$ K. It has C-type antiferromagnetic order where the magnetic moments of Co³⁺ ions aligning antiferromagnetically in the ab plane and antiferromagnetic yab layers stack ferromagnetically along the c axis⁴². The high-spin configuration of Co³⁺ ions ($S = 2$) has been reported⁴². The magnetic moments are $m = 3.24(2)\mu_B$ for $T = 5$ K and $m = 2.93(2)\mu_B$ at room temperature⁴². A reduction of the observed magnetic moment compared to the expected value $4\mu_B$ may be ascribed to the covalency of Co-O bonds. The bond valence sums (BVS) at 300K obtained in 42 were 3.14 for Bi and -2.13 for O2 corresponding to the oxidation states +3 and -2, respectively. The BVS values were 2.68 for Co and -1.57 for O1 indicating the covalency effects. The spontaneous polarization in BiCoO₃ of $179 \mu\text{C}/\text{cm}^2$ has been predicted from first-principle Berry-phase calculations⁴³. The experimental observation of a ferroelectric hysteresis loop is problematic since the resistivity appears too low for the large applied electric field. Therefore it was proposed that BiCoO₃ should be regarded as a pyroelectric rather than a ferroelectric material (in pyroelectrics the dipole moments can not be reoriented by external electric field)⁴². The C-type antiferromagnetic order with a reduced magnetic moment of $2.41 \mu_B$ have been also predicted from first-principle calculations⁴³. Spin-polarized calculations with C-type antiferromagnetic order for BiCoO₃ predicts an insulating ground state with an energy gap of 0.6 eV.

BiNiO₃ has been found to be an insulating antiferromagnet ($T_N = 300$ K)⁴⁴ with a heavily distorted triclinic symmetry $P\bar{1}$. The lattice constants are shown in Table I. X-ray powder diffraction data has revealed that Bi ions were disproportionately weighted towards Bi³⁺ and Bi⁵⁺ and therefore the oxidation state of the Ni ion was +2 rather than the expected +3^{44,45}. The Curie constant estimated from the magnetic susceptibility of BiNiO₃ is close to that expected for $S = 1$ rather than for $S = 1/2$ system. This fact as well as BVS confirms the divalent nature of Ni. The electronic structure of BiNiO₃ has been performed by the full-potential method within LDA+U ($U = 8$ eV, $J = 0.95$ eV) approximation with the G-type antiferromagnetic spin configuration⁴⁶. At ambient pressure a insulating solution with the charge-transfer gap of 0.8 eV was obtained in agreement with the value of 0.675 eV estimated from the electrical resistivity⁴⁴. From the powder neutron diffraction study it was found that the valence state of BiNiO₃ changes under pressure⁴⁶. Both neutron diffraction

measurements and BVS show that under pressure the charge disproportionate state melts leading to the simultaneous charge transfer from Ni to Bi, so that the high-pressure phase is metallic $\text{Bi}^{3+}\text{Ni}^{3+}\text{O}_3$. This transition takes place at 4 GPa pressure and structure changes to the GdFeO_3 -type with the $Pbnm$ symmetry⁴⁶. First-principle calculations also reproduce the metallic character of high-pressure phase.

IV. RESULTS AND DISCUSSION

A. Results of LSDA calculation

The electronic structure of BiMeO_3 ($Me = \text{Sc, Cr, Mn, Fe, Co, Ni}$) series was calculated within the local spin density approximation (LSDA)^{47,48} with a linearized muffin-tin orbitals basis (LMTO)⁴⁹ using the STUTTGART TB-LMTO program (version LMTO47). For all compounds the experimental atomic positions and lattice constants shown in Table I were used. For the spin-polarized calculations we used the experimentally determined magnetic structures described in previous paragraphs (for BiFeO_3 the G-type AFM order was assumed). The resulting energy gaps ($E_g^{\text{Calc.}}$) as well as magnetic moments are shown in Table V along with the available experimental data. For BiScO_3 , BiCrO_3 , BiFeO_3 and BiCoO_3 LSDA gives an insulating solution. For BiMnO_3 LSDA results in a half-metallic solution although the material is known to be an insulator. The metallic state of BiNiO_3 obtained with LSDA calculations is also in contrast with experimental observations. The failure of LSDA is due to the improper treatment of Coulomb correlations. It is well known that LSDA+U improves the description of correlation effects in transition metal oxides due to treating the strong Coulomb repulsion between localized d states by adding a Hubbard-like term to the effective potential⁵⁰. This calculation requires the Hubbard parameter U and exchange interaction J . Although these parameters can be calculated by constrained LDA method⁵¹ at present work we just take typical values of $U = 3$ eV, $J = 1$ eV for BiMnO_3 and $U = 8$ eV, $J = 1$ eV for BiNiO_3 .

The total and partial densities of states (DOS) obtained for BiMeO_3 series within LSDA and LSDA+U (for BiNiO_3 and BiMnO_3) are presented in Figures 1 and 2. One can see that the valence band for all BiMeO_3 compounds is formed by the Me $3d$ states hybridized with the O $2p$ states. The low lying states at energy about -10 eV comes from Bi $6s$ states,

the so-called “lone pair”. These states are only slightly hybridized with $2p$ states of oxygen.

TABLE V: The calculated ($E_g^{Calc.}$) and estimated from XES and XAS spectra (Δ_g) values of energy gap in comparison with the experimental data taken from literature ($E_g^{Lit.}$). The calculated magnetic moments on the Me ion (m_{Me}) along with experimental estimations ($m_{Me}^{Lit.}$) for $BiMeO_3$ compounds. The different values of magnetic moments in case of $Me = Cr, Mn, Ni$ correspond to the nonequivalent Me atoms in the unit cell.

Compound	$E_g^{Calc.}$ [eV]	Δ_g [eV]	$E_g^{Lit.}$ [eV]	m_{Me} [μ_B]	$m_{Me}^{Lit.}$ [μ_B]	Config. Me^{3+}
BiScO ₃	3.3	2.6	-	0	-	d^0
BiCrO ₃	0.88	1.4	-	2.63, 2.65	2.55 ⁸	d^3
BiMnO ₃	0.33	0.9	insulator ⁵²	3.65, 3.64	3.2 ¹⁸	d^4
BiFeO ₃	0.51	0.9	1.3 ⁶ , 2.5 ⁵³	3.54	3.75 ³²	d^5
BiCoO ₃	0.72	1.7	insulator ⁴²	2.41	3.24 ⁴²	d^6
BiNiO ₃	1.23	1.1	0.675 ⁴⁴	1.7; 1.67	1.76 ⁴⁵	d^7

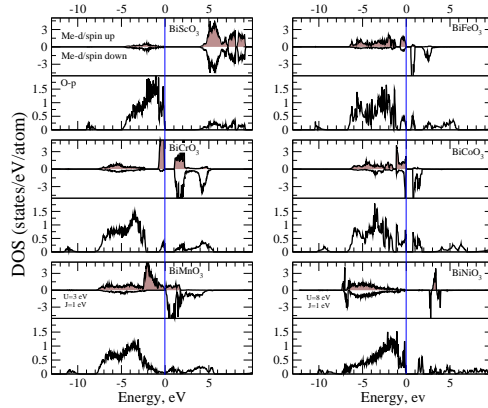


FIG. 1: LSDA (LSDA+U with $U = 3$ eV, $J = 1$ eV for BiMnO₃ and $U = 8$ eV, $J = 1$ eV for BiNiO₃) partial Me $3d$ and O $2p$ density of states for $BiMeO_3$ ($Me = Sc, Cr, Mn, Fe, Co, Ni$) compounds. The Fermi level corresponds to zero. (Colour in on-line version.)

BiScO₃, BiCrO₃, and BiMnO₃ all have a monoclinic structure and can be compared directly. The bondlengths for these three compounds are summarized in Table II. Although the space groups of these compounds are the same, the MeO_6 octahedra distortions are different for each and most pronounced in the case of BiMnO₃. The parameter Δ in Table II indicates the degree of MeO_6 octahedra distortion. The largest Δ corresponds to BiMnO₃

while in BiCrO_3 the CrO_6 octahedron is almost undistorted. The shortest Bi—O bond lengths also shrink from Sc to Mn. The oxygen atoms surrounding Bi do not form regular polyhedra so we take the six nearest neighbors and estimate the variations between the compounds. All three compounds display rather strong deviation from average Bi—O bond but the largest one is found for the BiScO_3 system. BiFeO_3 and BiCoO_3 have different structures. Five oxygen atoms surrounding the Co ion form a pyramid (see Table III). This pyramid is contracted so the distortion parameter is rather large. In BiFeO_3 the FeO_6 octahedron is less distorted than in BiMnO_3 system. The oxygen atoms are distributed around Bi in BiFeO_3 almost evenly while in BiCoO_3 rather irregular arrangement of oxygen atoms can be seen from Bi—O bondlengths shown in Table III. In Table IV the distances between Bi—O and Ni—O for BiNiO_3 are shown. The low symmetry of BiNiO_3 leads to the four nonequivalent Ni atoms and two nonequivalent Bi atoms in the unit cell. Among four Ni octahedra formed by oxygen atoms the one around Ni1 is the most distorted. The oxygen neighborhood around the Bi atoms is rather uniform.

For BiScO_3 and BiCrO_3 an insulating solution was obtained with LSDA calculations (see Figure 1). BiScO_3 has a formal electronic configuration d^0 and calculated energy gap of 3.3 eV. The valence band is formed by O $2p$ states while the conduction band is composed of Sc $3d$ states hybridized with O $2p$ states. BiCrO_3 has three electrons occupying t_{2g} orbitals (see Figure 1). The energy gap of 0.88 eV and magnetic moment of 2.63 and 2.65 μ_B (for two nonequivalent Cr atoms) was obtained in spin-polarized calculation in good agreement with the value 2.55 μ_B obtained in neutron diffraction experiments⁸. Both the valence and conduction bands are formed mainly by Cr $3d$ states with small admixture of O $2p$ states. LSDA+U produces the insulating state for ferromagnetically ordered BiMnO_3 in agreement with experiment (see Figure 1). The calculated magnetic moments for two nonequivalent Mn ions are 3.64 and 3.65 μ_B which is in agreement with experimental values shown in Table V. Both the O $2p$ and the Mn $3d$ bandwidths are wider than those of BiCrO_3 but the main contribution to the valence band comes from Mn $3d$ states. There is also a strong overlap of O $2p$ and Mn $3d$ bands.

LSDA calculations result in an insulating solution for BiFeO_3 with the energy gap of 0.51 eV. This is much smaller than experimental estimates^{6,53}. However the magnetic moment value of 3.54 μ_B is in good agreement with experiment (see Table V). The calculated DOS agrees well with the results of previous *ab initio* calculations⁴¹. Within LSDA the high spin

(HS) state for the d^5 configuration of Fe ion was obtained as shown in Figure 1. Both the valence and conduction bands are formed predominantly by Fe $3d$ states hybridized with O $2p$ states.

The LSDA calculations for BiCoO_3 suggest it is an insulator with an energy gap of 0.72 eV. We obtained HS state of d^6 electrons with magnetic moment of $2.41\mu_B$ which is smaller than $4\mu_B$ (expected for HS state) due to covalency effects.

With the LSDA+U method BiNiO_3 is insulator with an energy gap of 1.23 eV. This value is twice as large as the experimental result from Reference 44 but in good agreement with the present experimental estimation (see Table V). The values of the calculated magnetic moments given in Table V are in agreement with the experimental one. From the density of states it can be seen that the top of the valence band and the bottom of the conduction band are formed by Bi1 $6s$ and Bi2 $6s$ states hybridized with O $2p$ states. The occupancies calculated for the d states of the four non-equivalent Ni atoms in the LSDA+U calculation are 8.2, 8.36, 8.23, and 8.49 indicating that Ni has a 2+ valence which is in agreement with calculations performed in the literature⁴⁶.

B. Experimental results and discussion

The O K_α XES and O $1s$ XAS measurements of BiMeO_3 ($Me = \text{Sc, Cr, Mn, Fe, Co, Ni}$), which probe the occupied and vacant O $2p$ states, respectively, are presented in Figure 3. The fine structure and energy distribution of the O K_α XES matches the O $2p$ occupied DOS obtained from LSDA calculations (see Figure 2). The band gap for these materials was estimated using the peaks in the second derivative, this method has been shown to work well with O K_α XES and $1s$ XAS⁵⁴. A small amount of hybridization between the Bi $6s$ - and O $2p$ -states is visible at about 519 eV in all compounds, as suggested by the calculated O $2p$ -states.

The estimated energy gaps from the experimental spectra and the calculations are not exactly the same. This is expected, since LSDA calculations are known to provide a underestimation of the energy gap, and the LSDA+U calculations used a typical value for U rather than a material-specific value. We have found that the calculated energy gaps are mostly within 0.5 eV of the experimental energy gaps and, more importantly, the trend in the calculated energy gaps is essentially the same as that in the experimental energy gaps

for these materials. The energy gaps are shown in Figure 4, note the similar shape in the experimental and calculated curves.

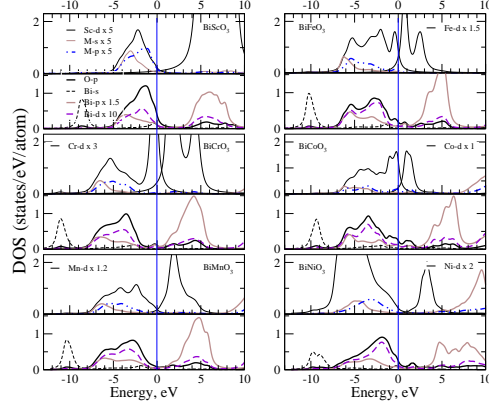


FIG. 2: Calculated LSDA (LSDA+U for BiMnO₃ and BiNiO₃) partial density of states for BiMeO₃ ($Me = \text{Sc, Cr, Mn, Fe, Co, Ni}$) compounds. The DOS have been convoluted with the Fermi step at $T = 300 \text{ K}$ and broadened by 0.3 eV using a Lorentzian function to mimic the experimental resolution. The Fermi level corresponds to zero. (Colour in on-line version.)

The comparison of the oxygen and iron X-ray spectra of BiFeO₃ with the calculated O $2p$ and Fe $3d$ DOSes is shown in Figure 5 and Figure 6, respectively (solid line). The Fermi level position for the Fe L_3 XES was determined using the XPS Fe $2p_{3/2}$ binding energy (710 eV)⁵⁵. In the absence of XPS O $1s$ data the O K_α XES is compared with O $2p$ DOS by alignment of Bi $6s$ related subbands. The LSDA calculation reproduces the energy position of the Fe L_3 XES (which probes occupied Fe $3d$ states) with respect to the Fermi level. On the other hand, the available LSDA+U calculations^{6,41} show a low-energy shift of Fe $3d$ band which contradicts the experimental Fe L_3 XES. The spectral weight of Fe $3d$ - and O $2p$ states is redistributed with increasing U value within LSDA+U calculations, as shown in Figures 5 and 6. As the U value rises the Fe $3d$ states are shifted to lower energies (Figure 6). At the same time the O $2p$ states (Figure 5) are shifted towards Fermi level. Taking this trend into account both the occupied O $2p$ - and Fe $3d$ states obtained with $U = 0 \text{ eV}$ are in better agreement with experimental spectra than the one calculated with a nonzero U . The Fe $L_{2,3}$ XES spectrum has some intensity at and just below the Fermi level while the O K_α XES spectrum indicates a clear energy gap (see the lower panel of Figure 5) in this energy region. In a recently published paper⁶ it is concluded that LSDA+U calculations ($U = 2 \text{ eV}$) are a better match to experimental Fe L_3 XES of BiFeO₃ than a LSDA (where

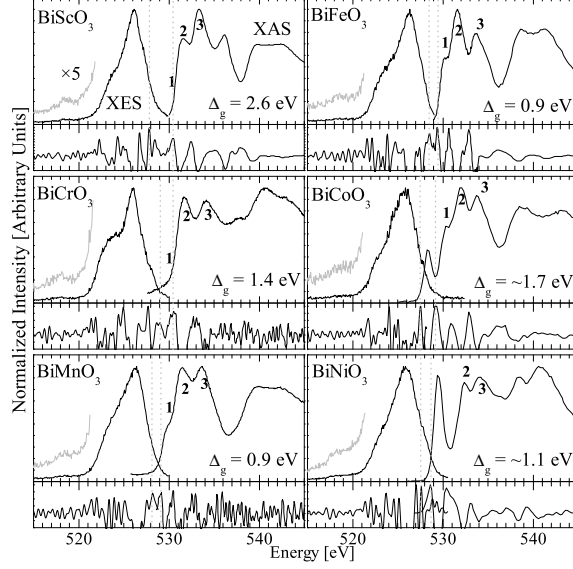


FIG. 3: Measured oxygen K_{α} X-ray emission spectra (XES) and O $1s$ X-ray absorption spectra (XAS) of BiMeO_3 compounds. The XAS is measured in total fluorescent yield (TFY) mode. The energy gap is estimated using the peaks in the second derivative, plotted below the corresponding spectra. The Bi $6s$ — O $2p$ hybridization peak at about 519 eV has been magnified by a factor of 5.

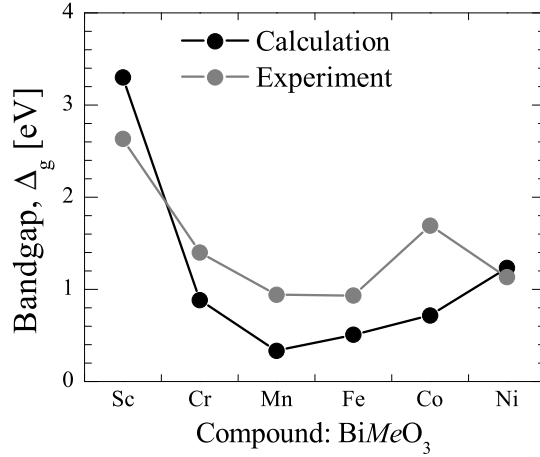


FIG. 4: The experimental (gray dots) and calculated (black dots) energy gaps for the BeMeO_3 compounds.

$U = 0$ eV) calculation. However, the comparison procedures used in matching calculations to experimental spectra are not described in Reference 6. Based on the comparison from Reference 6 one can estimate an XPS Fe $2p_{3/2}$ binding energy of 713 eV which contradicts

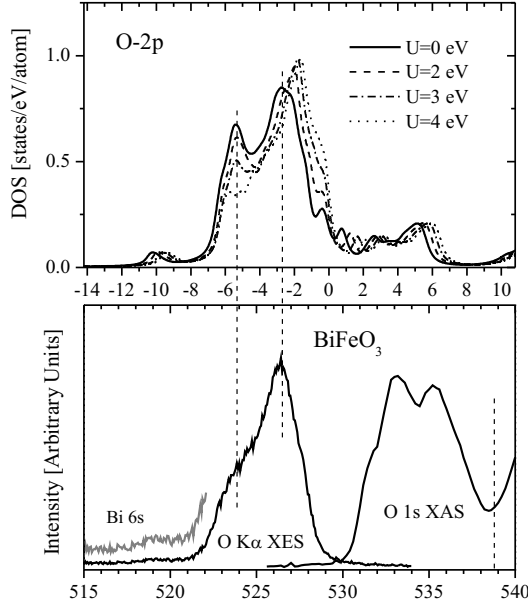


FIG. 5: The comparison between the O K_α XES and O $1s$ XAS (lower panel) and the LSDA+U O $2p$ DOS (upper panel) of BiFeO_3 . In the upper panel, the calculated LSDA+U O $2p$ DOS for several different values of U are shown. The O $2p$ DOSes were broadened by 0.3 eV using a Lorentzian function to mimic the experimental resolution. The Fermi level corresponds to zero.

the available experimental data (710 eV)⁵⁵.

As we have shown in Reference 56, the O $2p$ DOS for binary oxides of non-transition elements occupy a whole energy range of excited d states of cations, involved in formation of the chemical bonding in solids. In BiMeO_3 compounds, as seen in Figure 2, a correspondence of energies in the main maxima of O $2p$ and Bi $6d$ DOS occurs. The main maxima of the calculated $Me 3d$ DOS are also close to these energies. The non-bonding localized $3d$ states weakly mix with O $2p$ states near Fermi level.

All O K_α XES consist of low-energy subband located at ~ 2.5 eV with respect to the main maximum. As it was shown in Reference 56, the low-energy subband of O K_α XES of all binary oxides is directly connected with the s valence states of the cation. The energy separation of this subband from the main maximum depends in particular on the period number of Me . For ZnO it is ~ 2.4 eV, which coincides with the separation of subband from

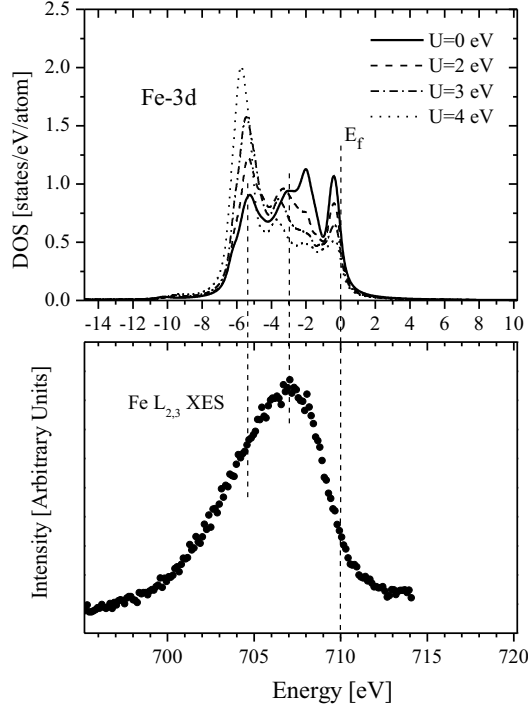


FIG. 6: The comparison between the Fe $L_{2,3}$ XES (lower panel) and the LSDA+U Fe $3d$ DOSes (upper panel) of BiFeO_3 . In the upper panel, the calculated LSDA+U Fe $L_{2,3}$ DOS for several different values of U are shown. The Fe $3d$ DOS has been convoluted with the Fermi step at $T = 300$ K and broadened by 0.3 eV using a Lorentzian to mimic the experimental resolution. The Fermi level corresponds to zero.

the main band of O K_α XES for BiMeO_3 compounds. The Bi $6s$ states are located ~ 5 eV below the $\text{Me } 4s$ states, this is why they hybridize only weakly with the O $2p$ states (see Figure 2).

The near edge fine structure of the O $1s$ XAS (see Figure 3) consists of three peaks (labeled as 1, 2 and 3) separated by $\sim 1.5 - 2$ eV for all compounds. There is a similar peak structure in the calculated unoccupied O $2p$ DOS (Figure 2) in spite of the fact that the band gap ($E_g^{\text{Calc.}}$) is not reproduced in LSDA calculations. Indeed, the lack of the appropriate energy gap does not effect the correct reproduction of the energy distance between the main maximum of the O K_α XES and the first peak of the O $1s$ XAS (~ 5 eV) in the LSDA+U calculations. This further demonstrates the well-known fact that O $2p$

states are less influenced by correlation effects than d states⁵⁴.

The O $1s$ XAS spectra of BiNiO_3 and BiCoO_3 show additional peaks near the Fermi level similar to those which were observed in the O $1s$ XAS of $\text{Li}_x\text{Ni}_{1-x}\text{O}$ ⁵⁷, LiCoO_2 ⁵⁸ and LaNiO_3 ⁵⁹. These additional peaks were attributed in References 57,59 to the formation of O $2p$ hole electronic states because of the energy disadvantage associated with a Ni^{3+} charge state. The Co^{3+} charge state is more stable, hence the intensity of the hole-like peak in BiCoO_3 is much lower than that in BiNiO_3 . Indeed, the “hole effect” in BiNiO_3 is even larger than that in $\text{Li}_x\text{Ni}_{1-x}\text{O}$ ⁵⁷. Among the materials studied in Reference 57 the intensity of the O $2p$ hole peak was found to be largest for $\text{Li}_{0.5}\text{Ni}_{0.5}\text{O}$ where the hole peak had $\sim 70\%$ of the intensity of the main maximum of the O $1s$ XAS. Similar intensity ratios have been reported for LaNiO_3 ⁵⁹. In BiNiO_3 , however, the relative intensity of the O $2p$ hole peak is about 100% of the intensity of the main O $2p$ band. The O $2p$ holes are created in order to maintain the neutrality of the compound with the Ni^{2+} valence state. They are clearly observed in the O $1s$ XAS for Ni oxides LaNiO_3 and BiNiO_3 . In the LSDA+U calculation the gap arises between the states predominantly formed by Bi $6s$ states strongly hybridized with O $2p$ states. The Ni atoms have a 2+ valency in agreement with experimental findings.

Now let us discuss the origin of ferroelectricity in BiMnO_3 and BiFeO_3 . From Figure 2 it is clear that the Bi $6s$ states in all compounds are not hybridized with the Bi $6p$ states. As was supposed in Reference 60, these Bi $6s$ lone pairs are slightly hybridized with O $2p$ states, and can induce dipole moment. However, we could not find any difference in degree of Bi $6s$ -O $2p$ hybridization for BiMnO_3 and BiFeO_3 compared to that of other BiMeO_3 compounds where no ferroelectricity is observed. The stereochemical activity of the Bi lone pair induces the electric moment but if the symmetry of the system includes inversion the net polarization turns to zero. The space group for the monoclinic structure of BiMnO_3 contains inversion while the rhombohedral BiFeO_3 has $R\bar{3}c$ symmetry without inversion. Therefore the origin of ferroelectricity in these two compounds seems to be different. In BiMnO_3 the emergence of electric moment is connected with inversion symmetry breaking by the AFM order induced by particular orbital order below $T = 474\text{K}$ ^{29,30}. Another scenario for the onset of electric moment is possible in BiFeO_3 : an extensive investigation of ferroelectricity in BiFeO_3 in the framework of density functional theory was reported in Reference 41. It was mentioned that the driving force of the ferroelectric distortion is the Bi lone pair. The calculated values of polarization agree well with experimental results³⁵.

Among the BiMeO_3 series there are three compounds with no inversion symmetry: BiMnO_3 (monoclinic structure, but inversion is broken by AFM order), BiFeO_3 (rhombohedral structure) and BiCoO_3 (tetragonal structure). The ferroelectric properties of the BiMnO_3 and BiFeO_3 are confirmed experimentally while a ferroelectric hysteresis loop has not yet been observed for BiCoO_3 . One possible reason could be a low resistivity to the applied electric field as was pointed out in Reference 42. The crystal structures of the BiScO_3 ($C2/c$), BiCrO_3 ($C2/c$), and BiNiO_3 ($P\bar{1}$) compounds include the inversion operation.

V. SUMMARY

In conclusion, the electronic structure of the BiMeO_3 ($Me = \text{Sc, Cr, Mn, Fe, Co, Ni}$) series was studied by soft X-ray emission and absorption spectroscopy. Experimental spectra were found to be in good agreement with spin-polarized electronic structure calculations. The presence of holes in the O $1s$ XAS spectrum of BiNiO_3 was attributed to the 2+ valency of Ni. For all BiMeO_3 ($Me = \text{Sc, Cr, Mn, Fe, Co, Ni}$) compounds the band gap values were estimated from O K_α XES and O $1s$ XAS spectra. In case of BiFeO_3 this estimation results in the band gap value ~ 0.9 eV. The X-ray spectra for multiferroic and nonmultiferroic compounds in the series do not reveal any difference in degree of Bi $6s$ -O $2p$ hybridization. It was concluded that for nonzero electric polarization the stereochemical activity of the Bi lone pair should be accompanied with the inversion symmetry breaking. This condition is satisfied in case of BiMnO_3 , BiFeO_3 and BiCoO_3 but the electric polarization arises due to the different reasons. In BiMnO_3 noncollinear magnetic order with AFM component breaks the inversion symmetry and allow net polarization. In BiFeO_3 the rhombohedral crystal structure does not contain inversion and the crucial role is played by Bi lone pairs. BiCoO_3 is supposed to be ferroelectric but a ferroelectric hysteresis loop has not been observed as of now so apparently BiCoO_3 should be considered as a pyroelectric material.

Acknowledgments

We acknowledge support of the Research Council of the President of the Russian Federation (Grants NSH-1929.2008.2, NSH-1941.2008.2 and MK-3227.2008.2(PZV)), the Russian Science Foundation for Basic Research (Project 08-02-00148), the Dynasty Foundation

(PZV), the Natural Sciences and Engineering Research Council of Canada (NSERC), and the Canada Research Chair program.

* Electronic address: john.mcleod@usask.ca

† Electronic address: pzv@ifmlrs.uran.ru

- ¹ G. Smolenskii, V. Isupov, A. Agranovskaya, and N. Kranik, *Sov. Phys. Solid State* **2**, 2651 (1961).
- ² G. Smolenskii, V. Yudin, E. Sher, and Y. E. Stolyпин, *Sov. Phys. JETP* **16**, 622 (1963).
- ³ J. F. Scott, *Nature Materials* **6**, 256 (2007).
- ⁴ N. A. Spaldin and M. Fiebig, *Science* **309**, 391 (2005).
- ⁵ C. Ederer and N. A. Spaldin, *Current Opinion in Solid State and Materials Science* **9**, 128 (2005).
- ⁶ T. Higuchi, Y.-S. Liu, P. Yao, P.-A. Glans, J. Guo, Z. W. C. Chang, W. Sakamoto, N. Itoh, T. Shimura, T. Yogo, et al., *Phys. Rev. B* **78**, 085106 (2008).
- ⁷ J.-S. Kang, S. W. Han, J.-G. Park, S. C. Wi, S. S. Lee, G. Kim, H. J. Song, H. Shin, W. Jo, and B. Min, *Phys. Rev. B* **71**, 092405 (2005).
- ⁸ A. A. Belik, S. Iikubo, K. Kodama, N. Igawa, S. Shamoto, and E. Takayama-Muromachi, *Chem. Mater.* **20**, 3765 (2008).
- ⁹ A. A. Belik, S. Iikubo, T. Yokosawa, K. Kodama, N. Igawa, S. Shamoto, M. Azuma, M. Takano, K. Kimoto, Y. Matsui, et al., *J. Am. Chem. Soc.* **129**, 971 (2007).
- ¹⁰ A. A. Belik, S. Iikubo, K. Kodama, N. Igawa, S. Shamoto, M. Maie, T. Nagai, Y. Matsui, S. Y. Stefanovich, B. I. Lazoryak, et al., *J. Am. Chem. Soc.* **128**, 706 (2006).
- ¹¹ J. J. Jia, T. A. Callcott, J. Yurkas, A. W. Ellis, F. J. Himpsel, M. G. Samant, J. Stöhr, D. L. Ederer, J. A. Carlisle, E. A. Hudson, et al., *Rev. Sci. Instrum.* **66**, 1394 (1995).
- ¹² T. Regier, J. Krochak, T. K. Sham, Y. F. Hu, J. Thompson, and R. I. R. Blyth, *Nucl. Instrum. Meth. A* **582**, 93 (2007).
- ¹³ R. E. Eitel, C. A. Randall, T. R. Shrout, P. W. Rehrig, W. Hackenberger, and S.-E. Park, *Jpn. J. Appl. Phys.* **40**, 5999 (2001).
- ¹⁴ F. Sugawara, S. Iida, Y. Syono, and S. Akimoto, *J. Phys. Soc. Jpn.* **25**, 1553 (1968).
- ¹⁵ S. Niitaka, M. Azuma, M. Takano, E. Nishibori, M. Takata, and M. Sakata, *Solid State Ionics*

- 172**, 557 (2004).
- ¹⁶ A. A. Belik, N. Tsujii, H. Suzuki, and E. Takayama-Muromachi, *Inorg. Chem.* **46**, 8746 (2007).
 - ¹⁷ E. Montanari, G. Calestani, L. Righi, E. Gilioli, F. Bolzoni, K. S. Knight, and P. G. Radaelli, *Phys. Rev. B* **75**, 220101(R) (2007).
 - ¹⁸ A. M. dos Santos, A. K. Cheetham, T. Atou, Y. Syono, Y. Yamaguchi, K. Ohoyama, H. Chiba, and C. N. R. Rao, *Phys. Rev. B* **66**, 064425 (2002).
 - ¹⁹ N. A. Hill, P. Battig, and C. Daul, *J. Phys. Chem. B* **106**, 3383 (2002).
 - ²⁰ N. A. Hill and K. M. Rabe, *Phys. Rev. B* **59**, 8759 (1999).
 - ²¹ R. Seshadri and N. A. Hill, *Chem. Mater.* **13**, 2892 (2001).
 - ²² A. M. dos Santos, S. Parashar, A. R. Raju, Y. S. Znao, A. K. Cheetham, and C. N. R. Rao, *Solid State Commun.* **122**, 49 (2002).
 - ²³ T. Shishidou, N. Mikamo, Y. Uratani, F. Ishii, and T. Oguchi, *J. Phys.: Condens. Matter* **16**, S5677 (2004).
 - ²⁴ T. Atou, H. Chiba, K. Ohoyama, Y. Yamaguchi, and Y. Syono, *J. Solid State Chem.* **145**, 639 (1999).
 - ²⁵ A. M. dos Santos, A. K. Cheetham, T. Atou, Y. Syono, Y. Yamaguchi, K. Ohoyama, H. Chiba, and C. N. R. Rao, *Phys. Rev. B* **66**, 064425 (2002).
 - ²⁶ E. Montanari, G. Calestani, A. Migliori, M. Dapiaggi, F. Bolzoni, R. Cabassi, and E. Gilioli, *Chem. Mater.* **17**, 6457 (2005).
 - ²⁷ T. Shishidou (2007), *private communication*.
 - ²⁸ P. Baettig, R. Seshadri, and N. A. Spaldin, *J. Am. Chem. Soc.* **129**, 9854 (2007).
 - ²⁹ I. V. Solovyev and Z. V. Pchelkina, *New J. Phys.* **10**, 073021 (2008).
 - ³⁰ I. V. Solovyev and Z. V. Pchelkina, *Pis'ma v ZhETF.* **89**, 701 (2009).
 - ³¹ G. A. Smolenskii and I. Chupis, *Sov. Phys. Usp.* **25**, 475 (1982).
 - ³² I. Sosnowska, W. Schäfer, W. Kockelmann, K. H. Andersen, and I. O. Troyanchuk, *Appl. Phys. A* **74**, S1040 (2002).
 - ³³ I. Sosnowska, T. Peterlin-Neumaier, and E. Steichele, *J. Phys. C* **15**, 4835 (1982).
 - ³⁴ J. R. Teague, R. Gerson, and W. J. James, *Solid State Commun.* **8**, 1073 (1970).
 - ³⁵ J. Wang, J. B. Neaton, H. Zheng, V. Nagarajan, S. B. Ogale, B. Liu, D. Viehland, V. Vaithyanathan, D. G. Schlom, U. V. Waghmare, et al., *Science* **299**, 1719 (2003).
 - ³⁶ J. Li, J. Wang, M. Wuttig, and R. Ramesh, *Appl. Phys. Lett.* **84**, 5261 (2004).

- ³⁷ K. Y. Yun, D. Ricinschi, T. Kanashima, M. Noda, and M. Okuyama, *Jpn. J. Appl. Phys.* **43**, L647 (2004).
- ³⁸ R. D. King-Smith and D. Vanderbilt, *Phys. Rev. B* **47**, 1651 (1993).
- ³⁹ D. Vanderbilt and R. D. King-Smith, *Phys. Rev. B* **48**, 4442 (1993).
- ⁴⁰ R. Resta, *Rev. Mod. Phys.* **66**, 899 (1994).
- ⁴¹ J. B. Neaton, C. Ederer, U. V. Waghmare, N. A. Spaldin, and K. M. Rabe, *Phys. Rev. B* **71**, 014113 (2005).
- ⁴² A. A. Belik, S. Iikubo, K. Kodama, N. Igawa, S. Shamoto, S. Niitaka, M. Azuma, M. Takano, F. Izumi, and E. Takayama-Muromachi, *Chem. Mater.* **18**, 798 (2006).
- ⁴³ Y. Uratani, T. Shishidou, F. Ishii, and T. Oguchi, *Jpn. J. Appl. Phys.* **44**, 7130 (2005).
- ⁴⁴ S. Ishiwata, M. Azuma, M. Takano, E. Nishibori, M. Takata, M. Sakata, and K. Kato, *J. Mater. Chem.* **12**, 3733 (2002).
- ⁴⁵ S. J. E. Carlsson, M. Azuma, Y. Shimakawa, M. Takano, A. Hewat, and J. P. Attfield, *J. Solid State Chem.* **181**, 611 (2008).
- ⁴⁶ M. Azuma, S. Carlsson, J. Rodgers, M. G. Tucker, M. Tsujimoto, S. Ishiwata, S. Isoda, Y. Shimakawa, M. Takano, and J. P. Attfield, *J. Am. Chem. Soc.* **129**, 14433 (2007).
- ⁴⁷ W. Kohn and L. J. Sham, *Phys. Rev.* **140**, A1133 (1965).
- ⁴⁸ L. Hedin and B. I. Lundqvist, *J. Phys. C* **4**, 2064 (1971).
- ⁴⁹ O. K. Andersen, *Phys. Rev. B* **12**, 3060 (1975).
- ⁵⁰ V. I. Anisimov, F. Aryasetiawan, and A. I. Lichtenstein, *J. Phys.: Condens. Matter* **9**, 767 (1997).
- ⁵¹ O. Gunnarsson, O. K. Andersen, O. Jepsen, and J. Zaanen, *Phys. Rev. B* **39**, 1708 (1989).
- ⁵² T. Kimura, S. Kawamoto, I. Yamada, M. Azuma, M. Takano, and Y. Tokura, *Phys. Rev. B* **67**, 180401 (2003).
- ⁵³ F. Gao, Y. Yuan, K. F. Wang, X. Y. Chen, F. Chen, J.-M. Liu, and Z. F. Ren, *Appl. Phys. Lett.* **89**, 102506 (2006).
- ⁵⁴ E. Z. Kurmaev, R. G. Wilks, A. Moewes, L. D. Finkelstein, S. N. Shamin, and J. Kuneš, *Phys. Rev. B* (2008).
- ⁵⁵ P. Kharel, S. Talebi, B. Ramachandran, A. Dixit, V. M. Naik, M. B. Sahana, R. Naik, M. S. R. Rao, and G. Lawes, *J. Phys.: Condensed Matter* **21**, 036001 (2009).
- ⁵⁶ J. A. McLeod, R. G. Wilks, N. A. Skorikov, L. D. Finkelstein, M. Abu-Samak, E. Z. Kurmaev,

and A. Moewes (2009), cond-mat/0908.1581v1.

- ⁵⁷ P. Kuiper, G. Kruizinga, J. Ghijsen, G. A. Sawatzky, and H. Verweij, Phys. Rev. Lett. **62**, 221 (1989).
- ⁵⁸ V. R. Galakhov, V. V. Karelina, D. G. Kellerman, V. S. Gorshkov, N. A. Ovechkina, and M. Neumann, Phys. Solid State **44**, 266 (2002).
- ⁵⁹ M. Abbate, G. Zampieri, F. Prado, A. Caneiro, J. M. Gonzalez-Calbet, and M. Vallet-Regi, Phys. Rev. B **65**, 155101 (2002).
- ⁶⁰ J. van den Brink and D. I. Khomskii, J. Phys.: Condensed Matter **20**, 434217 (2008).